

Understanding Multiplication

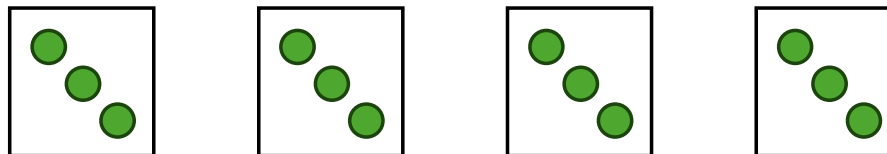
Multiplication is Repeated Addition

Multiplication is adding the same number again and again.

Example: 3×4

Means add 3 to itself 4 times.

$$3 + 3 + 3 + 3$$



It takes a long time to repeatedly add the same number.

Multiplication is a **shortcut** for repeated addition.

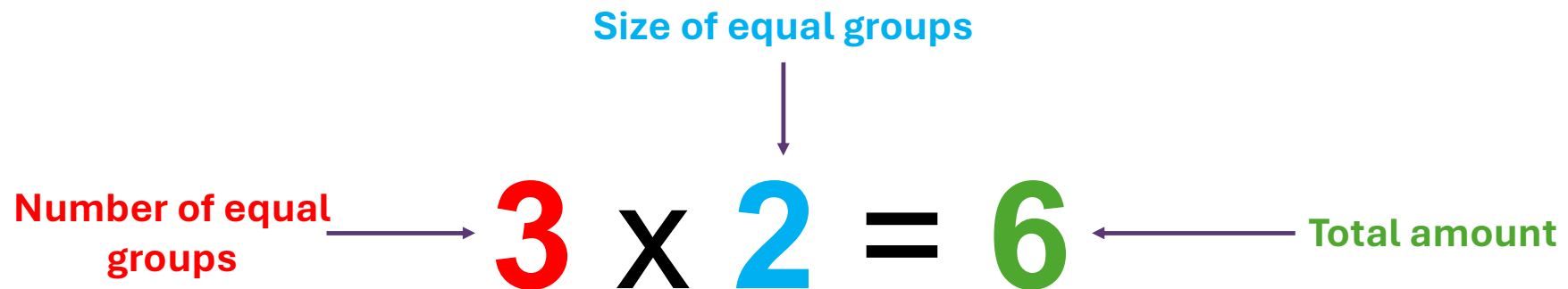
The Language of Multiplication

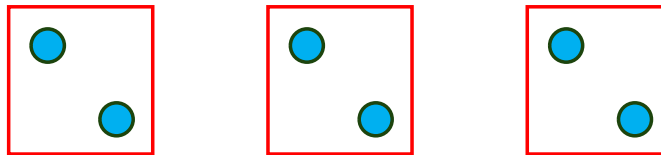
Size of equal groups

Number of equal groups

$$3 \times 2 = 6$$

Total amount

A diagram illustrating the components of the multiplication equation 3 x 2 = 6. The number 3 is red, 2 is blue, and 6 is green. An arrow points from the text 'Number of equal groups' to the red 3. Another arrow points from the text 'Size of equal groups' to the blue 2. A third arrow points from the text 'Total amount' to the green 6.



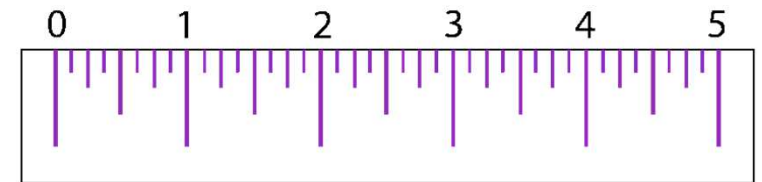
I have **three groups** of **2 counters**, I have **6 counters** in total

Times Tables You Must Know

The 1, 2, 5 and 10 times tables are the foundation facts. You must know them off by heart. You can learn them using dot patterns, Cuisenaire rods and number lines. All other times-table facts can be worked out from these facts and from understanding that multiplication is commutative (you can swap the order of the numbers).

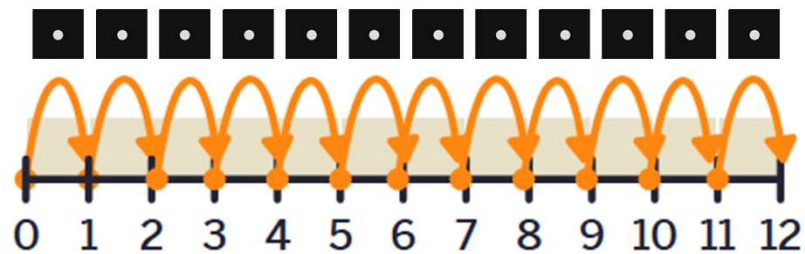


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Times Tables You Must Know: One Times Tables



$$1 \times 1 = 1$$

$$2 \times 1 = 2$$

$$3 \times 1 = 3$$

$$4 \times 1 = 4$$

$$5 \times 1 = 5$$

$$6 \times 1 = 6$$

$$7 \times 1 = 7$$

$$8 \times 1 = 8$$

$$9 \times 1 = 9$$

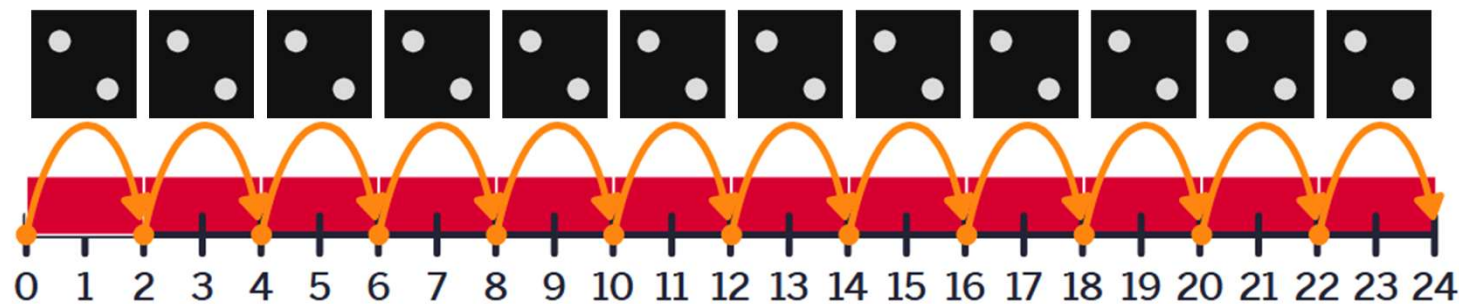
$$10 \times 1 = 10$$

$$11 \times 1 = 11$$

$$12 \times 1 = 12$$

Times Tables You Must Know: Two Times Tables

Two Times Tables



$$1 \times 2 = 2$$

$$2 \times 2 = 4$$

$$3 \times 2 = 6$$

$$4 \times 2 = 8$$

$$5 \times 2 = 10$$

$$6 \times 2 = 12$$

$$7 \times 2 = 14$$

$$8 \times 2 = 16$$

$$9 \times 2 = 18$$

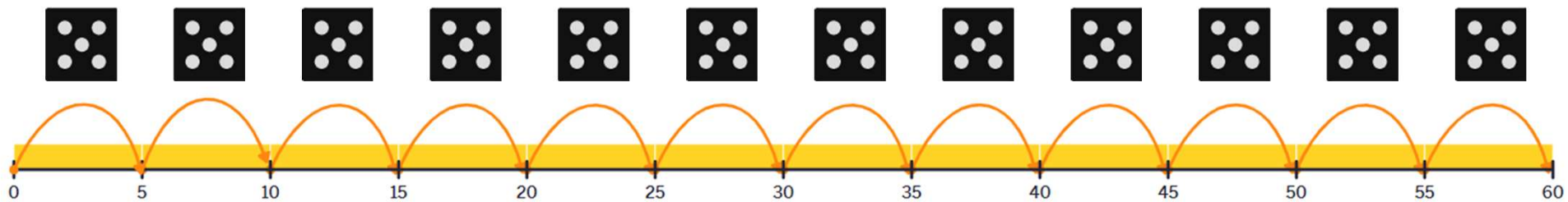
$$10 \times 2 = 20$$

$$11 \times 2 = 22$$

$$12 \times 2 = 24$$

Times Tables You Must Know: Five Times Tables

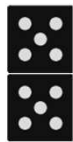
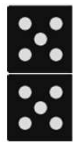
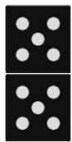
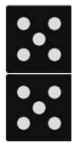
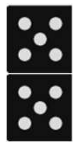
Five Times Tables



- $1 \times 5 = 5$
- $2 \times 5 = 10$
- $3 \times 5 = 15$
- $4 \times 5 = 20$
- $5 \times 5 = 25$
- $6 \times 5 = 30$
- $7 \times 5 = 35$
- $8 \times 5 = 40$
- $9 \times 5 = 45$
- $10 \times 5 = 50$
- $11 \times 5 = 55$
- $12 \times 5 = 60$

Times Tables You Must Know: Ten Times Tables

Ten Times Tables



$1 \times 10 = 10$
 $2 \times 10 = 20$
 $3 \times 10 = 30$
 $4 \times 10 = 40$
 $5 \times 10 = 50$
 $6 \times 10 = 60$
 $7 \times 10 = 70$
 $8 \times 10 = 80$
 $9 \times 10 = 90$
 $10 \times 10 = 100$
 $11 \times 10 = 110$
 $12 \times 10 = 120$

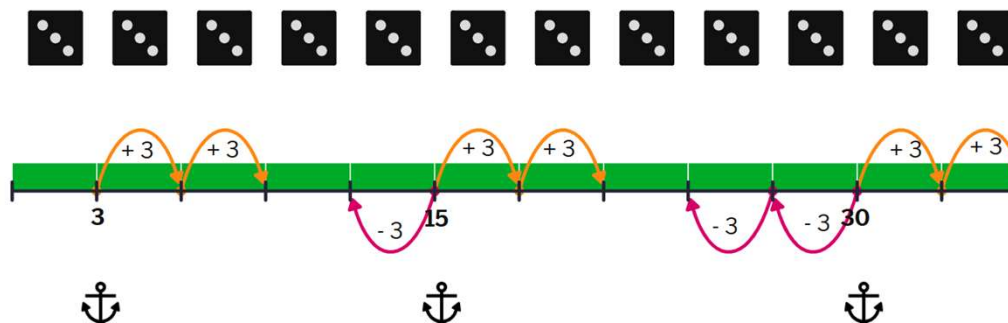
Working Out the Other Times Tables

All other multiplication facts can be reasoned from $1 \times n$, $5 \times n$, and $10 \times n$ by adding or subtracting in small steps. Use flashcards to practice finding the closest anchor and reasoning forwards and backwards from there.

Reasoning patterns that derive all other tables

- $2 \times n = (1 \times n) + (1 \times n)$
- $3 \times n = (2 \times n) + (1 \times n)$
- $4 \times n = (5 \times n) - (1 \times n)$
- $6 \times n = (5 \times n) + (1 \times n)$
- $7 \times n = (5 \times n) + (2 \times n)$
- $8 \times n = (10 \times n) - (2 \times n)$
- $9 \times n = (10 \times n) - (1 \times n)$
- $11 \times n = (10 \times n) + (1 \times n)$
- $12 \times n = (10 \times n) + (2 \times n)$

Example: Three Times Tables



$1 \times 3 = 3$
 $2 \times 3 = 3 + 3 = 6$
 $3 \times 3 = 6 + 3 = 9$
 $4 \times 3 = 15 - 3 = 12$
 $5 \times 3 = 15$
 $6 \times 3 = 15 + 3 = 18$
 $7 \times 3 = 15 + 6 = 21$
 $8 \times 3 = 30 - 6 = 24$
 $9 \times 3 = 30 - 3 = 27$
 $10 \times 3 = 30$
 $11 \times 3 = 30 + 3 = 33$
 $12 \times 3 = 30 + 6 = 36$

Drawing A Multiplication Square

Make good use of extra time in your maths exams by drawing a multiplication square. You can use it to solve multiplication and division problems and to identify square numbers and equivalent fractions.

To draw a multiplication square:

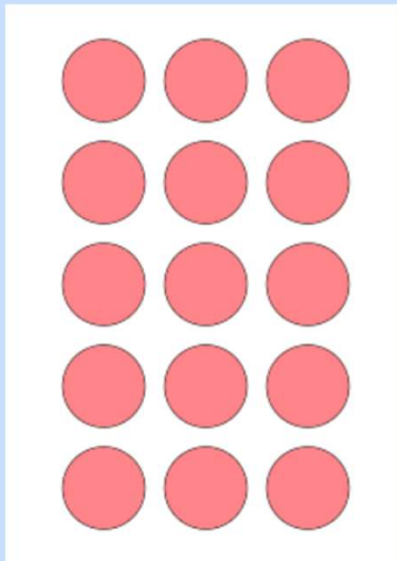
- Draw the grid and label the rows and columns.
- Fill in the parts you already know.
- Begin with the multiplication tables you are most confident with, such as the 1s, 2s, 5s and 10s.
- Then move on to the 9s, 11s and 12s, using the patterns in these tables to help you complete more of the grid.
- After that, work through the 3s, 4s and 6s.
- Leave the 7s and 8s until last, as these are often the trickiest.
- Highlight the square numbers once the grid is complete.
- Practise regularly until you can fill in the whole grid quickly and accurately.

[illegible]

$$a \times b = b \times a$$

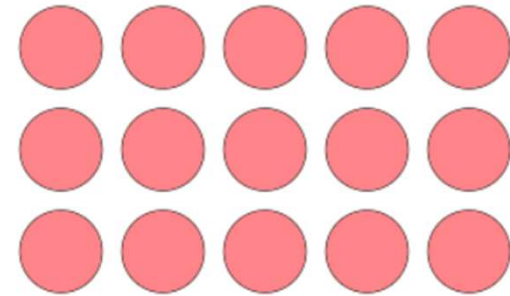
The commutative property of multiplication states that changing the order of the factors does not change the product. In other words:
 $a \times b = b \times a$. Whether you multiply 5×3 or 3×5 , the result is still 15.

$$5 \times 3 = 15$$



5 rows of 3 equals 15
 $5 \times 3 = 15$

$$3 \times 5 = 15$$



3 rows of 5 equals 15
 $3 \times 5 = 15$

Long Multiplication: Grid Method

The grid method is a way of multiplying large numbers by breaking them down into smaller, easier-to-manage chunks. It uses a grid to organise the calculation.

How to use the grid method

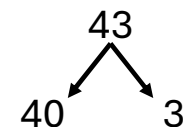
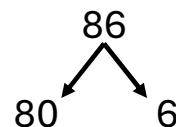
- **Estimate.** Rounding each number to 1 significant figure and estimate the answer.
- **Partition.** Split each number into its place value parts.
- **Draw a grid.** Label the columns with one number's place value parts and the rows with the other number's place value parts.
- **Multiply.** Multiply the value at the start of each row by the value at the top of each column. Write each product in the correct box.
- **Add.** Add all the products to find the total.
- **Check.** Compare your answer with your estimate to check that it's reasonable.
- **State.** Clearly write the final answer.

Example: $86 \times 43 =$

$86 \rightarrow 90$

$43 \rightarrow 40$

$9 \times 4 = 36$, therefore $90 \times 40 = 3600$



	80	6
$\times$		
40	3200	240
3	240	18

$$\begin{array}{r} 3200 \\ 240 \\ 240 \\ + 18 \\ \hline 3698 \end{array} \text{ Estimate } \checkmark$$

$$\mathbf{86 \times 43 = 3698}$$

Acknowledgements

- Images were created using free virtual manipulatives by Amplify available at [Polypad.com](https://www.polypad.com).